

# Dynamic Recovery over Large Scale Graph-Structured Data with Subgraphs

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**Abstract:** In this paper, we propose a novel Part-level Regularized Semi-Nonnegative coding (PRSN) approach to construct a discriminative graph benefiting from the part-level graph regularizer. Specifically, with the low-rank decomposition via SNMF, our method can well uncover the global structure of the multiple subspace of the data. Meanwhile, it preserves the local intrinsic information by virtue of part-level similarity measurement. Finally, with the iteratively optimized data representation matrix  $Z$ , the label information can be effectively propagated to the remaining unlabeled data.

**Introduction:** The main objective of this paper, a novel graph construction approach for graph based learning, including data clustering and semi-supervised classification. By taking advantages of low-rank coding and sparsification constraints, we jointly learned symmetric and sparse graphs. Graphs have been widely applied in modeling the relationships and structures in real-world applications. Graph construction is the most critical part in these models, while how to construct an effective graph is still an open problem. In this paper, we propose a novel approach to graph construction based on two observations. First, by virtue of recent advances in low-

rank subspace recovery, the similarity between every two samples evaluated in the low-rank code space is more robust than that in the sample space. Second, a sparse and balanced graph can greatly increase the performance of learning tasks, such as label propagation in graph based semi-supervised learning. The k-NN sparsification can provide fast solutions to constructing unbalanced sparse graphs, and b-matching constraint is a necessary route for generating balanced graphs. These observations motivate us to jointly learn the low-rank codes and balanced (or unbalanced) graph simultaneously. In particular, two non-convex models are built by incorporating k-NN constraint and b-matching constraint into the low-rank representation model, respectively. We design a majorization-minimization augmented Lagrange multiplier (MM-ALM) algorithm to solve the proposed model.

**Existing System:** In unsupervised and semi-supervised learning, the algorithms usually show effective performance on data that obey the smoothness, cluster or manifold assumptions.

**Methodologies:** Databases and settings, Problem formulation & optimization, Spectral Clustering with Graph, Semi-Supervised Classification with Graph.

**Databases and settings:** In this module, we randomly generate dataset and process with these data. we randomly select 50 datasets of every class in the A and B tables, 100 datasets from each class in the C database, and use all the datasets of ORL database.

**Semi-Supervised Classification with Graph:** We first normalize all the images to be unit-norm as shown in Algorithm 2. All methods are repeated 10 times, and each time we randomly select a subset of images for each individual to create a labeled sample set. We can observe that our two graphs obtain better performance than other graphs. Even though Ours-I graph is unbalanced, it performs better than our previous work LRCB graph that is balanced. The reason is that Ours-I, as well as Ours-II, reformulates the rank-minimization model to obtain a new similarity metric, which is the key during graph construction.

**Data Collection with Part-level regularized graph:** The graph regularizer helps generate a more sparse and discriminative coefficient matrix  $Z$  [21], [28]. As we know, the similar data points should also have similar coefficients  $Z$ , so the graph regularizer is designed to transfer such local intrinsic structure via a similarity matrix  $S$ . The common way to measure the similarity is via various distance metrics based on  $Z$ . However, the common way is NOT the best choice in this case. We consider part-level representation coefficient  $H$  can uncover much richer information from underlying sample structure. In order to differentiate the similarity matrix learned over part-level representation  $H$  from the conventional one, we denote the

novel similarity as  $SP$ , and its corresponding Lapidarian matrix as  $LP$ .

**Optimization and Complexity Analysis:** In this section, we discuss the time complexity of our model. For simplicity, assume  $X$  is a  $n \times n$  matrix. The time-consuming components of Algorithm 1 are the semi nonnegative matrix factorization operation in Step 1, and matrix multiplication and inverse operations in Step 2. As discussed in, the computation complexity for SNMF is  $m(n2p + np^2)$  for updating variable  $W \in Rn \times p$ , where  $m$  is the number of iterations to convergence (we set  $m = 10$  in our experiment) and  $p$  is the dimension of  $W$  (we set it as the rank of  $Z$ ). The computation complexity of updating variable  $H \in Rp \times n$  for SNMF is  $3mn2p$ . Thus, the total complexity for Step 1 is of order  $(4mn2p + mnp^2)$ . Generally, each matrix multiplication and inverse operation take  $O(n^3)$ . Thus, the order of time cost for Step 2 is  $O(n^3)$ . To sum up, the time complexity of our method is  $O(n^3 + 4mn2p + mnp^2)$ .

#### Algorithm:

**Input:** data matrix  $X$ , parameter  $\lambda_1, \lambda_2, k$

**Initialize:**  $Z_0 = E_0 = W_0 = H_0 = LP_0 = 0$ ,

$Y_{1,0} = Y_{2,0} = 0, \mu_0 = 10^{-6}, \mu_{\max} = 106_{-} = 10^{-4}, \rho = 1.3, t = 0$ .

while not converged do

1. Fix the others and update  $W_{t+1}, H_{t+1}$  using Eq. (6)
2. Fix the others and update  $Z_{t+1}$  using Eq. (7)
3. Fix the others and update  $LP_{t+1}$  using  $k$ -NN.
4. Fix the others and update  $E_{t+1}$  using Eq. (8).
5. Update the multiplier  $Y_{1,t+1}, Y_{2,t+1}$  by  
 $Y_{1,t+1} = Y_{1,t} + \mu(X - XZ_{t+1} - E_{t+1})$ ,  
 $Y_{2,t+1} = Y_{2,t} + \mu(\mathbf{1}TnZ_{t+1} - \mathbf{1}Tn)$ ,
6. Update the parameter  $\mu$  by  $\mu = \min(\rho\mu, \mu_{\max})$
7. Check the convergence condition by

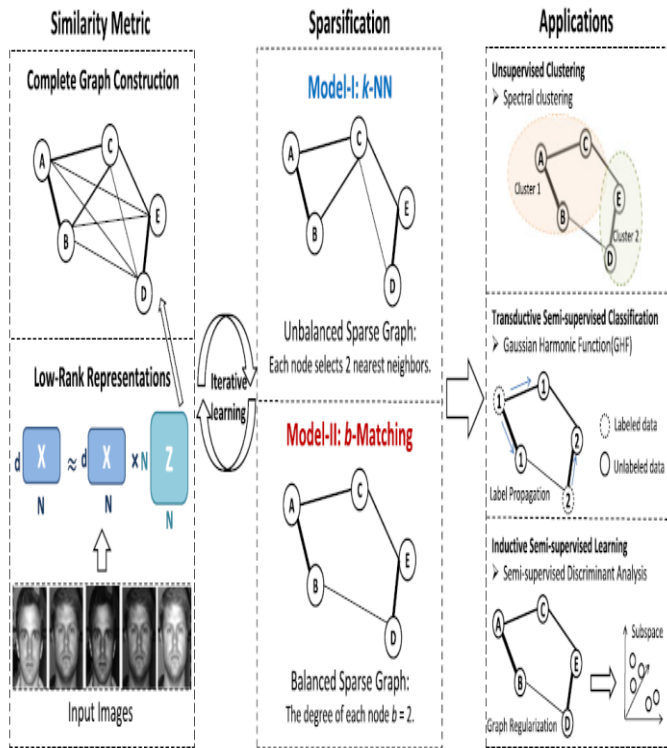
$$X - XZt+1 - Et+1_{\infty} < \dots, 1TnZt+1 - 1Tn_{\infty} < \dots$$

8.  $t = t + 1$ .

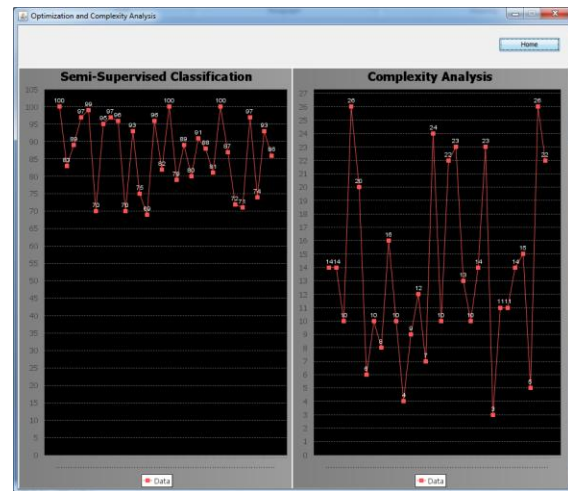
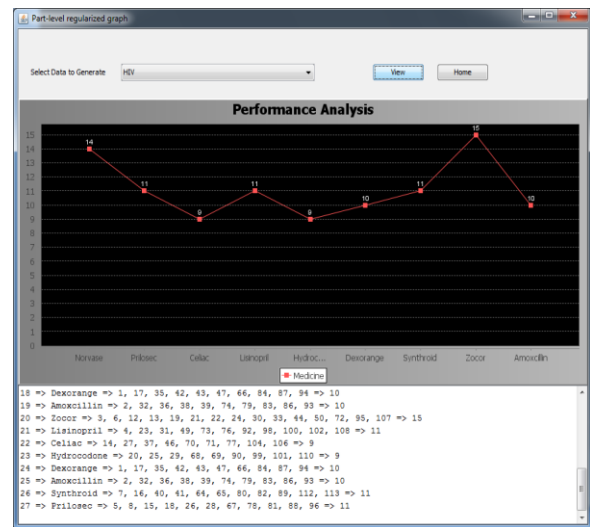
end while

**Output:**  $Z, W, H, E, LP$

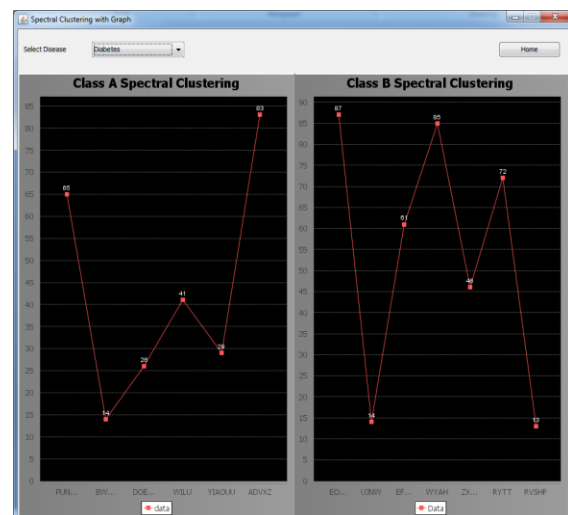
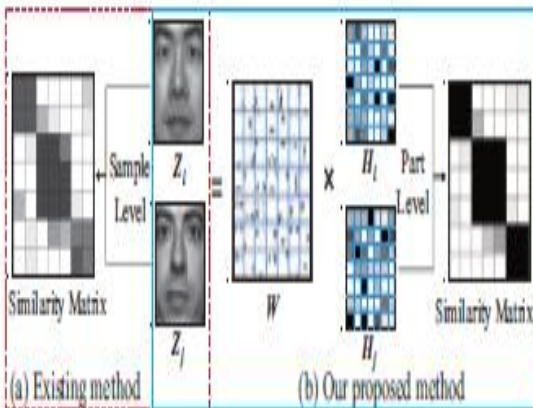
**Architecture:**



**Example:**



**Existing method and proposed method:**



**Conclusion:** In this paper, we have proposed a novel graph construction approach for graph based learning, including data clustering and semi-supervised classification. By taking advantages of low-rank coding and sparsification constraints (i.e., k-NN and b-matching), we jointly learned symmetric and sparse graphs. We also designed novel optimisation algorithms to solve the proposed models.

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