

Image Denoising of Various Images using Wavelet Transform and Thresholding Techniques

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Abstract - Generally the Gaussian and salt Pepper noise occurred in images of different quality due to random variation of pixel values. To denoise these images, it is necessary to apply various filtering techniques. So far there are lots of filtering methods proposed in literature which includes the haar, sym4, and db4 Wavelet Transform based soft and hard thresholding approach to denoise such type of noisy images. This work analyses exiting literature on haar, db4 and sym4 Wavelet Transform for image denoising with variable size images from self generated grayscale database generated from various image sources such as satellite images(NASA), Engineering Images and medical images. However this new proposed Denoising method shows signs of satisfactory performances with respect to previous literature on standard indices like Signal-to-Noise Ratio (SNR), Peak Signal to Noise Ratio (PSNR) and Mean Square Error (MSE). Literature indicates that Wavelet transform represents natural image better than any other transformations. Therefore, Wavelet coefficient can be used to improve quality of true image and from noise. The aim of this work to eliminate the Gaussian and salt Pepper noise in wavelet transform domain. Subsequently a soft and hard threshold based denoising algorithm has been developed. Finally, the denoised image was compared with original image using some quantifying statistical indices such as MSE, SNR and PSNR for different noise variance which the experimental results demonstrate its effectiveness over previous method.

Key Words: Image Denoising, Gaussian noise, salt Pepper noise, Wavelet transforms, Image Thresholding techniques, Signal-to-Noise Ratio (SNR), Peak Signal to Noise Ratio (PSNR), Mean Square Error (MSE).

1. INTRODUCTION

The image usually has noise which is not easily eliminated in image processing. According to actual image characteristic, noise statistical property and frequency spectrum distribution rule, people have developed many methods of eliminating noises, which

approximately are divided into space and transformation fields. The space field is data operation carried on the original image, and processes the image grey value, like neighborhood average method, wiener filter, center value filter and so on. The transformation field is management in the transformation field of images, and the coefficients after transformation are processed. Then the aim of eliminating noise is achieved by inverse transformation, like wavelet transform [1], [2]. Successful exploitation of wavelet transform might lessen the noise effect or even overcome it completely [3]. There are two main types of wavelet transform - continuous and discrete [2]. Because of computers discrete nature, computer programs use the discrete wavelet transform. The discrete transform is very efficient from the computational point of view. In this paper, we will mostly deal with the modeling of the wavelet transform coefficients of natural images and its application to the image denoising problem. The denoising of a natural image corrupted by Gaussian noise is a classic problem in signal processing [4]. The wavelet transform has become an important tool for this problem due to its energy compaction property [5]. Indeed, wavelets provide a framework for signal decomposition in the form of a sequence of signals known as approximation signals with decreasing resolution supplemented by a sequence of additional touches called details [6][7]. Denoising or estimation of functions, involves reconstituting the signal as well as possible on the basis of the observations of a useful signal corrupted by noise [8] [9] [10] [11]. The methods based on wavelet representations yield very simple algorithms that are often more powerful and easy to work with than traditional methods of function estimation [12]. It consists of decomposing the observed signal into wavelets and using thresholds to select the coefficients, from which a signal is synthesized [5]. Image denoising still remains a challenge for researchers because noise removal introduces artifacts and causes blurring of the images. This paper describes different methodologies for noise reduction (or denoising) giving an insight as to

which algorithm should be used to find the most reliable estimate of the original image data given its degraded version.

2. REVIEW OF SELECTED LITERATURE ON WAVELET TRANSFORM BASED IMAGE DENOISING

F. Xiaoa et al. [6] presented a technique Wavelet-based image denoising which is the foundation of wavelet-based de-noising through thresholding. To explore properties of various thresholding techniques in wavelets denoising several natural gray scale test images like Lina, Barbara of size 512 X 512 at different noise levels are 10, 20, 30, 35 with soft thresholding and semi-soft thresholding with discrete Mayer filter having 4th level decomposition are used to evaluate these threshold selection algorithms are used to explore various Properties of image denoising algorithm and quantitative comparison between these techniques through MSE and PSNR (Peak Signal-to-Noise Ratio). Based on their results authors conclude that BayesShrink and Feature-Adaptive Shrink are the best wavelet-based denoising methods in methods.

Z. Weipeng et al. [7] Presented method with combining two-dimensional discrete wavelet transform and bilateral denoising is introduced for this purpose two images of coal-mine refuge chamber in different scenes are selected as original images with sizes of 352 X 288 pixels. First the wavelet transform is adopted to break down the image of safety enclosure and low frequency component of subject image remains unchanged. Then, 3 high-frequency elements are activated by bilateral filtering, and the image is reconstructed. While supplying better optical effect and ultimately terminate that integrating wavelet transform and bilateral filtering collectively, can in effect destruct image noises of refuge chamber, and result comparison given in this paper depending on Comparison of information entropy, standard deviation and mean gradient after applying bilateral filtering based on wavelet transform. When coal mine disaster happen proposed method will guide the emergency deliverance and assurance the coal-mine safety production.

C. chen et al. [8] proposed method which uses the digital complex ridgelet transform to denoise some standard images such as lina, MRI image and Thumb Impression image having Gaussian white noise. Hard thresholding of the complex ridgelet coefficients is used. their experiment Results show that this new method performs VisuShrink, the ordinary ridgelet image denoising, and wiener2 filter both in terms of peak signal-to-noise ratio and in visual quality. In particular, this method preserves sharp edges better while

removing white noise. Complex ridgelets could be applied to curvelet image denoising as well.

A. Jaiswal et al. [9]proposed a method worked with de-noising of user generated image, saltpepper and Gaussian noise. Remaining work is organized in four steps first image is denoised by filtering method, second images is denoised by wavelet based techniques using thresholding, third hard thresholding and filtering method applied simultaneously on noisy image, at last results of PSNR (peak signal to noise ratio) and MSE (mean square error) are calculated by comparing all cases. Experiments are performed on the 512 X 512 noisy images with noise having noise variance 0.04, output of median filter, Wiener filter, hard thresholding and hard thresholding plus median filtering implemented on the basis of PSNR, MSE and visual quality of image. The filtering and wavelet thresholding technique jointly gives good agreement of PSNR and MSE than applying Bior, Hard thresholding plus Wiener filter method.

G. Gao [10] proposed a method controls both the structural and statistical belongings of microarray of stranded images lina, barbras and Gaussian noise added which acting for wavelet based microarray picture denoising and for shrinking of microarray images. The shrinking scheme is unusual in its use of approximate (rather than perfect) textual matter. Proposed method brings forth smaller overall bits per pixel when compared with Micro Zip the best-known microarray compression algorithm. Given the assets of data typically bring forth by microarray based on experimentation. Further granted the important amount of noise that is ordinary in such experiments, method acting for removing (or at least reducing) the noise, in front further analysis using the microarray images.

H. Rabbani et. al [11] proposed denoising model is able to capture the heavy-tailed nature of wavelet coefficients and the local parameters model the intrascale dependency between the coefficients. For that purpose standard images are taken such as ship, mri and gaussian noise is added and proved a novel method for image/video denoising based on designing a maximum a posteriori (MAP) estimator, which relies on the mixture distributions for each wavelet coefficient in each sub band. This method employs two different versions of expectation maximization (EM) algorithm to find the parameters of mixture model and compare our new method with other image denoising techniques that are based on (1) non mixture pdfs that are not local, (2) non mixture pdfs with local variances, (3) mixture pdfs

without local parameters and (4) methods that consider both heavy-tailed and locality properties. The technique is best among the best reported in the literature both visually and peak signal-to-noise ratio (PSNR). Because 3-D complex wavelet transform provides a motion-based multiscale decomposition for video, proposed algorithm has very good performance without explicitly using motion estimation.

V. Bruni et al. [12] Presents scheme for simultaneous compression and denoising of images using WISDOW-Comp (Wavelet based Image and Signal Denoising via Overlapping Waves Compression). However, atoms can be also used for achieving compression. In selected images such as lina, ship etc the core of WISDOW-Comp consists of recovering wavelet details by exploiting wavelet low frequency information. Therefore, just the approximation band and significance map of atoms absolute maxima have to be encoded and sent to the decoder for recovering a cleaner as well as compressed version of the image such as lina. Results show that WISDOW-Comp outperforms the state of the art of compression based denoisers in terms of both rate and distortion.

3. PROPOSED ALGORITHM

An image is a rectangular grid of pixels. It has a definite height and a definite width counted in pixels. Each pixel is square and has a fixed size on a given display. However different computer monitors may use different sized pixels and different types such as gray scale, color image (.jpeg, .gif, .png, .tiff etc.). The noise will reduce the quality of the images (the different noised images are showed in Figure 3 such as Gaussian and salt pepper noise) To clear noise from image is called as image denoising one goal in image restoration or denoising is to remove the noise from the image in such a way that the original image is discernible of course, noise is in the eye of the beholder; One approach is to decide that features that exist on a very small scale in the image are noise, and that removing these while maintaining larger features might help clean things up. Different Wavelet Transforms such as Db4, Sym4 and Haar used in project work Daubechies constructed the first wavelet family of scale functions that are orthogonal and have finite vanishing moments, i.e., compact support. This property insures that the number of non-zero coefficients in the associated filter is finite. This is very useful for local analysis. The Haar wavelet is the simplest wavelet transform. It is also the only symmetric wavelet in the Daubechies family and the only one that has an explicit

expression in discrete form. Haar wavelets are related to a mathematical operation called Haar transform such as one of the brightest stars in the world of wavelet research, invented what called compactly supported orthonormal wavelets are thus making discrete wavelet analysis practicable. The names of the Daubechies family wavelets are written dbN, where N is the order [10], and db the surname of the wavelet. Symlet Wavelet, also known as “least asymmetric” wavelet, defines a family of orthogonal wavelets. Symlet Wavelet[n] is defined for any positive integer n. The scaling function (Ψ) and wavelet function (Φ) have compact support length of $2n$. The scaling function has n vanishing moments. Symlet Wavelet can be used with such functions as Discrete Wavelet Transform and Wavelet Phi, etc. In symN, N is the order. Some author’s use $2N$ instead of N. Thresholding is the simplest method of image denoising. In this from a gray scale image, thresholding can be used to create binary image. Thresholding is used to segment an image by setting all pixels whose intensity values are above a threshold to a foreground value and all the remaining pixels to a background value. Thresholding is mainly divided into two categories hard and soft thresholding.

Image processing is required to remove unwanted noise so that the quality of the processed image does not deteriorate. Generally, the noise is removed using some specified filters. Several methods have been reported to remove such noises from the stationary digital images. Discrete wavelet transform (DWT) is one of the recent wavelet transforms used in image processing. DWT decomposes an image into different sub images as shown in figure below.

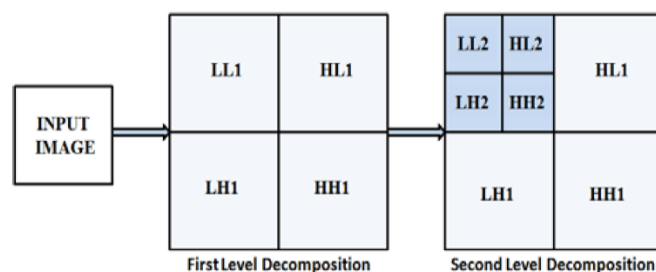


Figure 1: First and Second level of Image decomposition.

Denoising algorithm using DWT requires the decomposition of noised images to get the wavelet coefficients [9]. These coefficients are then denoised with wavelet threshold. Finally, inverse transform is applied to the coefficients and get denoised image [9].

This process is called the reconstruction of an image using decomposition.

3.1 Image Denoising using Wavelet and Thresholding is carried out in following steps.

To denoise the image by using wavelet transform, the following steps are carried out as per algorithm shown in figure 2, For the experimentation variable size images from various image sources such as satellite images(NASA), Engineering Images and medical images are taken in to consideration.

Step 1: Select any one original image from MATLAB database for example original lina image from database is selected as shown in figure 3.

Step 2: Guassian noise at the variance of 0.01 or salt peeper noise at the variance of 0.1 is added in to original lina image from wavelet toolbox for example Gaussian noise of variance 0.01 and Salt pepper noise of variance 0.1 is added in to selected image from wavelet toolbox as shown in figure 4.

Step 3: These Noisy images are decomposed using different wavelet transforms such as db4, haar and sym4 for example haar Wavelet Transform is applied to these noisy images

Step 4: First level or second level decomposition is applied to these noisy image. In the first level of decomposition, the image is split into 4 sub bands, namely the HH, HL, LH and LL sub bands. The HH sub band gives the diagonal details of the image; the HL and LH sub bands give the horizontal and vertical features respectively. The LL sub band is the low resolution residual consists of low frequency components and its sub bands are further split at higher levels of decomposition as shown in figure 1. In Wavelet Sub bands as the level increases the coefficients of sub band becomes smoother.HL2 is smoother than HL1 and so threshold value should be smaller than for HL1 for example first and second level of decomposition for lina image is shown in figure 6.

Step 5: We have performed Soft and Hard Thresholding at each decomposition level of an image for different wavelet transforms. At each level the value of threshold is different for example at the end the inverse of the wavelet transform has been performed to get the denoised image as shown in figure 7.

Step 6: Finally the inverse of the wavelet transform has been performed to get the denoised image as shown in figure 7 and The performance of various wavelet transforms has been compared with the help of various parameters such as Peak signal to Noise Ratio (PSNR), Signal to Noise Ratio (SNR) and Mean Square Error (MSE), figure 8 shows complete denoised step wise result for lina.

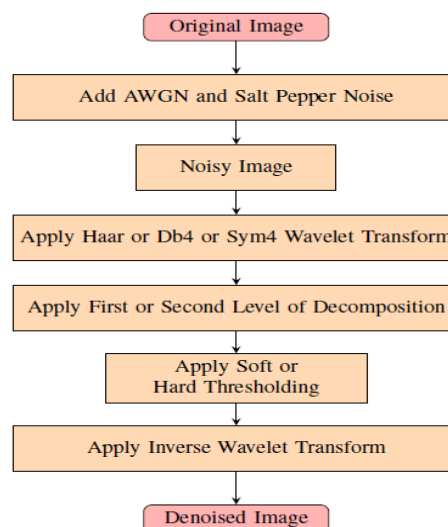


Figure 2: Wavelet Denoising Algorithm form Haar, Db4 and Sym4.



Figure 3: Selected original lina Image from MATLAB database.



a) Leena Image with Gaussian Noise



b) Leena with Salt Peeper Noise

Figure 4: Noisy lina Image a) lina with AWGN .01 variance and b) lina with Salt Peeper .1 variance.

4. EXPERIMENTAL RESULT AND DISCUSSION

Two parameters, PSNR (peak signal to noise ratio) and MSE (Mean square Error) are calculated for all the denoised images.

4.1 Mean Square Error (MSE):

Mean Square Error (MSE) is defining as the average of square of the error. Error is difference between desire quantity and estimated quantity. The Mean Square Error (MSE) provides a means of choosing the best estimator. We also calculate Root Mean Square Deviation taking the square root of Mean Square Error (MSE), it is also good statistic parameter for measure

quality of image. Having a Mean Square Error of zero (0) is ideal. Lower the MSE produces good denoising result, The Mean Square Error (MSE) is defined and used to calculate error metrics used to compare the various image compression techniques are the Mean Square Error (MSE).

$$\text{Mean Square Error (MSE)} = \sum_{i=j=0}^N \frac{[f(i,j) - F(i,j)]^2}{N^2}$$

Where f (i,j) is the original image, F (i,j) is the approximated version (which is actually the decompressed image) and N or M are the dimensions of the images.

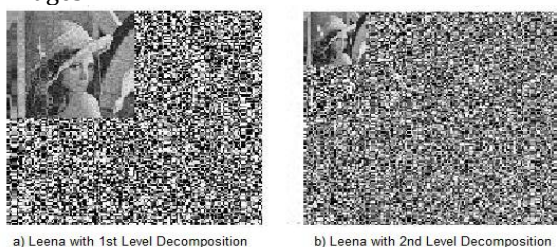
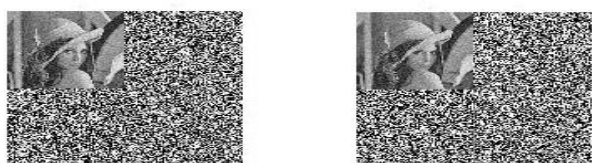


Figure 5: Level of decomposition a) lina with 1st level of decomposition b) lina with 2nd level of decomposition.

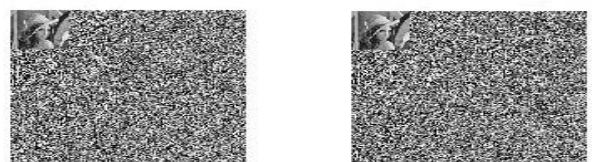


a) Using 1st Level Decomposition b) Using 2st Level Decomposition

Figure 6: lina Image a) Soft thresholding with 1st level Decomposition b) Hard thresholding with 1st level Decomposition c) Soft thresholding with 2nd level Decomposition d) Hard thresholding with 2nd level Decomposition.



a) 1st Level Decomposition (Soft Thresholding) b) 1st Level Decomposition (Hard Thresholding)



c) 2nd Level Decomposition (Soft Thresholding) d) 2nd Level Decomposition (Hard Thresholding)

Figure 7: Denoised lina Images a and b) with 1st level Decomposition c and d) with 2nd level decomposition.



Figure 8: Result of AWGN noisy lina using haar second level Decomposition with Soft thresholding.

4.2 Peak Signal to Noise Ratio (PSNR):

The Peak Signal-to-Noise Ratio (PSNR) is defined as a ratio between the maximum possible power of a signal and the noise power that affects the fidelity of its representation. PSNR is usually expressed in terms of the logarithmic decibel scale. The PSNR is most commonly used as a measure of quality of reconstruction of lossy compression for image compression. It is most easily defined via the Mean Square Error (MSE) which for two mxn monochrome images i and k where one of the images is considered a noisy approximation. Two of the error metrics used to compare the various image compression techniques are the Mean Square Error (MSE) and the Peak Signal to Noise Ratio (PSNR). The MSE is the cumulative squared error between the compressed and the original image, whereas PSNR is a measure of the peak error. The mathematical formulae for the two are:

$$\text{Mean Square Error (MSE)} = \sum_{i=j=0}^N \frac{[f(i,j) - F(i,j)]^2}{N^2}$$

The PSNR is defined as:

$$\text{PSNR} = 10 \log_{10} \left(\frac{\text{MAX}_I^2}{\text{MSE}} \right) = 20 \log_{10} \left(\frac{\text{MAX}}{\text{MSE}} \right)$$

Here, MAX_I is the maximum possible pixel value of the image. When the pixels are represented using 8 bits per sample, this is 255. More generally, when samples are represented using linear PCM with B bits per sample, MAX_I is 2^B - 1. Higher Peak signal to noise ratio produces good denoising results. Above figure 9 and figure 10 shows that Different Values of MSE and PSNR

for Selected images such as lina, Barbara, cameraman, Runner and Handshake, Grayscale Images with variable sizes are used for experimentation. Using proposed algorithm it is clear that PSNR values are not same for haar, db4 and sym4 wavelet transform. Out of these three sym4 shows high PSNR and Lowest MSE vales.

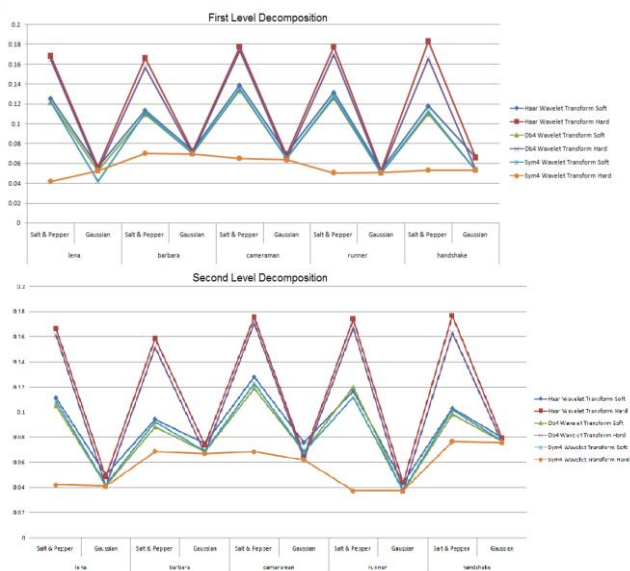


Figure 9: MSE Values of selected 5 Images with Hard and Soft Thresholding and First and Second Level of Decomposition.

5. CONCLUSION

In this paper several well known algorithms for denoising natural images were investigated and their performance was comparatively assessed. A new algorithm based on the haar, db4 and sym4 wavelet transform was developed. Its performance was shown to be competitive with or exceeding the performance of other algorithms. In addition, it has been shown to the advantage of implementation simplicity. There are different types of noises that may corrupt a natural image in real life, such as Gaussian noise and salt pepper noise etc. However, both salt pepper and white Gaussian noise was considered because of its simplicity. A major part of the thesis was devoted to the review, implementation and performance assessment of published image denoising algorithms based on various techniques including the haar, db4 and sym4 Wavelet transform. The Wavelet transform and its characteristics were studied and as per result and comparison, and previous literature say lower MSE of images gives good denoising result mean clear denoised image and higher PSNR values produces good quality of decomposed image it is

concluded that out of three haar db4 and sym4 wavelet transform sym4 gives lowest MSE values (0.0373) for the different images and highest PSNR value (62.4179) as compared to haar and db4.

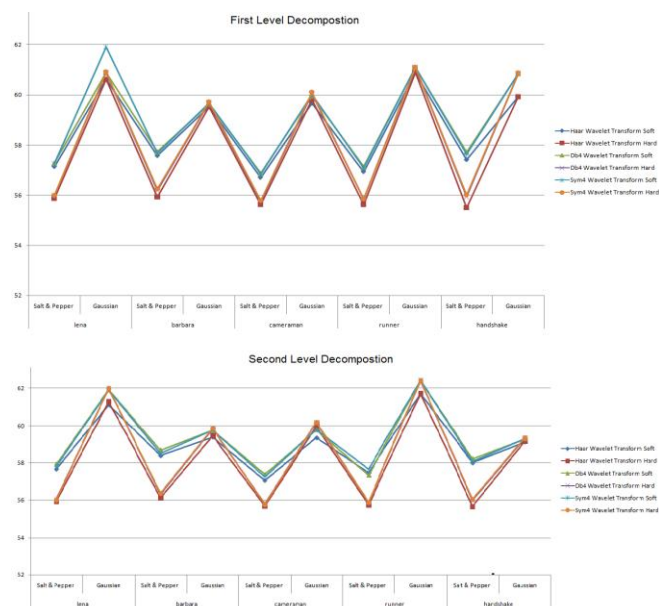


Figure 10: PSNR Values of selected 5 Images with Hard and Soft Thresholding and First and Second Level of Decomposition.

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